Package: PenCoxFrail (via r-universe)

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Description Different regularization approaches for Cox Frailty Models by penalization methods are provided.
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bs.design	Generate a B-spline design matrix

Description

The function generates a B-spline design matrix with equidistant knots for given degree of the splines and number of basis functions.

Usage

```
bs.design(x, x1, xr, spline.degree, nbasis, comp = NULL)
```

Arguments

X	the positions	where spline to	be evaluated.
---	---------------	-----------------	---------------

x1 lower intervall boundary where spline functions are relevant.
xr upper intervall boundary where spline functions are relevant.

spline.degree (polynomial) degree of the B-splines.

nbasis number of basis functions used.

comp Specify if only specific columns of the B-spline design matrix should be re-

turned. Default is NULL and the whole B-spline design matrix is returned.

Value

The B-spline design matrix is returned.

Author(s)

```
Andreas Groll Groll@math.lmu.de>
```

See Also

```
pencoxfrail
```

```
x <- rnorm(100)
B <- bs.design(x=x, xl=min(x), xr=max(x), spline.degree=3, nbasis=5)</pre>
```

coxFL A full likelihood approach for Cox Frailty Models.

Description

A full likelihood approach for Cox Frailty Models based on the full likelihood is provided.

Usage

```
coxFL(fix=formula, rnd=NULL, vary.coef=NULL, data, control = list())
```

Arguments

fix	a two-sided linear formula object describing the unpenalized fixed (time-constant) effects part of the model, with the response on the left of a ~ operator and the terms, separated by + operators, on the right. The response must be a survival object as returned by the Surv function.
rnd	a two-sided linear formula object describing the random-effects part of the model, with the grouping factor on the left of a ~ operator and the random terms, separated by + operators, on the right.Default is NULL, so no random effects are present.
vary.coef	a one-sided linear formula object describing the time-varying effects part of the model, with the time-varying terms, separated by $+$ operators, on the right side of a \sim operator.Default is NULL, so no time-varying effects are incorporated.
data	the data frame containing the variables named in the three preceding formula arguments.
control	a list of control values for the estimation algorithm to replace the default values returned by the function coxlassoControl. Defaults to an empty list.

Details

The coxFL algorithm is designed to investigate the effect structure in the Cox frailty model, which is a widely used model that accounts for heterogeneity in time-to-event data. Since in survival models one has to account for possible variation of the effect strength over time, some features can incorporated with time-varying effects.

Package: pencoxfrail
Type: Package
Version: 1.1.2
Date: 2023-08-25
License: GPL-2
LazyLoad: yes

for loading a dataset type data(nameofdataset)

Value

Generic functions such as print, predict, plot and summary have methods to show the results of the fit.

The predict function uses also estimates of random effects for prediction, if possible (i.e. for known subjects of the grouping factor). Either the survival stepfunction or the baseline hazard (not cumulative!) can be calculated by specifying one of two possible methods: method=c("hazard", "survival"). By default, for each new subject in new.data an individual stepfunction is calculated on a prespecified time grid, also accounting for covariate changes over time. Alternatively, for new.data a single vector of a specific (time-constant) covariate combination can be specified.

Usage: predict(coxlasso.obj,new.data,time.grid,method=c("hazard","survival"))

The plot function plots all time-varying effects, including the baseline hazard.

call a list containing an image of the coxlasso call that produced the object.

baseline a vector containing the estimated B-spline coefficients of the baseline hazard. If

the covariates corresponding to the time-varying effects are centered (and standardized, see coxlassoControl), the coefficients are transformed back to the

original scale.

time.vary a vector containing the estimated B-spline coefficients of all time-varying ef-

fects. If the covariates corresponding to the time-varying effects are standardized (see coxlassoControl) the coefficients are transformed back to the origi-

nal scale.

coefficients a vector containing the estimated fixed effects.

ranef a vector containing the estimated random effects.

Q a scalar or matrix containing the estimates of the random effects standard devi-

ation or variance-covariance parameters, respectively.

Delta a matrix containing the estimates of fixed and random effects (columns) for each

iteration (rows) of the main algorithm (i.e. before the final re-estimation step is

performed, see details).

Q_long a list containing the estimates of the random effects variance-covariance param-

eters for each iteration of the main algorithm.

iter number of iterations until the main algorithm has converged.

knots vector of knots used in the B-spline representation.

Phi.big large B-spline design matrix corresponding to the baseline hazard and all time-

varying effects. For the time-varying effects, the B-spline functions (as a function of time) have already been multiplied with their associated covariates.

time.grid the time grid used in when approximating the (Riemann) integral involved in the

model's full likelihood.

m number of metric covariates with time-varying effects.

m2 number of categorical covariates with time-varying effects.

Author(s)

Andreas Groll Groll@statistik.tu-dortmund.de>

References

Groll, A., T. Hastie and G. Tutz (2016). Regularization in Cox Frailty Models. Ludwig-Maximilians-University. *Technical Report* 191.

See Also

```
coxFLControl,Surv,pbc
```

```
## Not run:
data(lung)
# remove NAs
lung <- lung[!is.na(lung$inst),]</pre>
# transform inst into factor variable
lung$inst <- as.factor(lung$inst)</pre>
# just for illustration, create factor with only three ph.ecog classes
lung$ph.ecog[is.na(lung$ph.ecog)] <- 2</pre>
lung$ph.ecog[lung$ph.ecog==3] <- 2</pre>
lung$ph.ecog <- as.factor(lung$ph.ecog)</pre>
fix.form <- as.formula("Surv(time, status) ~ 1 + age + ph.ecog + sex")</pre>
coxFL.obj <- coxFL(fix=fix.form, data=lung,</pre>
                 control=list(print.iter=TRUE, exact = 1))
coef(coxFL.obj)
# For comparison: coxph
coxph.1 <- coxph(fix.form , data=lung)</pre>
coef(coxph.1)
# now add random institutional effect
coxFL.obj2 <- coxFL(fix=fix.form, rnd = list(inst=~1),</pre>
               data=lung, control=list(print.iter=TRUE, exact = 1))
coef(coxFL.obj2)
# print frailty Std.Dev.
print(coxFL.obj2$Q)
# print frailties
print(coxFL.obj2$ranef)
# For comparison: coxph
fix.form.cox <- update(fix.form, ~ . + frailty(inst, distribution="gaussian"))</pre>
coxph.2 <- coxph(fix.form.cox , data=lung)</pre>
coef(coxph.2)
# print frailty Std.Dev.
print(sqrt(coxph.2$history[[1]]$history[nrow(coxph.2$history[[1]]$history), 1]))
# print frailties
print(coxph.2$frail)
```

```
# now fit a time-varying effect for age
fix.form <- as.formula("Surv(time, status) ~ 1 + ph.ecog + sex")</pre>
vary.coef <- as.formula("~ age")</pre>
coxFL.obj3 <- coxFL(fix=fix.form,vary.coef=vary.coef,</pre>
              data=lung, control=list(print.iter=TRUE))
summary(coxFL.obj3)
# show fit
plot(coxFL.obj3)
# predict survival curve of new subject, institution 1 and up to time 300
pred.obj <- predict(coxFL.obj2, newdata=data.frame(inst=1, time=NA, status=NA, age=26,</pre>
              ph.ecog=2, sex=1), time.grid=seq(0,300,by=1))
# plot predicted hazard function
plot(pred.obj$time.grid,pred.obj$haz,type="1",xlab="time",ylab="hazard")
# plot predicted survival function
plot(pred.obj$time.grid,pred.obj$survival,type="1",xlab="time",ylab="survival")
## specify a larger new data set
new.data <- data.frame(inst=c(1,1,6), time=c(20,40,200),
      status=c(NA,NA,NA), age=c(26,26,54), ph.ecog=c(0,0,2), sex=c(1,1,1))
## as here no frailties have been specified, id.var needs to be given!
pred.obj2 <- predict(coxFL.obj3, newdata=new.data,id.var = "inst")</pre>
# plot predicted hazard functions (for the available time intervals)
# for individual 1 and 3
plot(pred.obj2$time.grid[!is.na(pred.obj2$haz[,1])],
      pred.obj2$haz[,1][!is.na(pred.obj2$haz[,1])],
      type="1",xlab="time",ylab="hazard",xlim=c(0,200),
      ylim=c(0,max(pred.obj2$haz,na.rm=T)))
lines(pred.obj2$time.grid[!is.na(pred.obj2$haz[,3])],
      pred.obj2$haz[,3][!is.na(pred.obj2$haz[,3])],
      col="red",lty=2,)
# plot predicted survival functions (for the available time intervals)
# for individual 1 and 3
plot(pred.obj2$time.grid[!is.na(pred.obj2$survival[,1])],
    pred.obj2$survival[,1][!is.na(pred.obj2$survival[,1])],
    type="1",xlab="time",ylab="hazard",xlim=c(0,200),
   ylim=c(0,max(pred.obj2$survival,na.rm=T)))
lines(pred.obj2$time.grid[!is.na(pred.obj2$survival[,3])],
      pred.obj2$survival[,3][!is.na(pred.obj2$survival[,3])],
      col="red",lty=2,)
## End(Not run)
```

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coxFLControl	Control Values for coxFL fit	
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Description

The values supplied in the function call replace the defaults and a list with all possible arguments is returned. The returned list is used as the control argument to the coxFL function.

Usage

```
coxFLControl(start = NULL, index=NULL, q_start = NULL, conv.eps = 1e-3,
                          standardize = FALSE, center = FALSE,
                          smooth=list(nbasis = 6, penal = 1e+2),
                          print.iter = FALSE, max.iter = 100,
                          exact = NULL, xr = NULL, eps = 1e-3, ...)
```

Arguments

start	a vector of suitable length containing starting values for the spline-coefficients
	of the baseline hazard and the time-varying effects, followed by the fixed and
	random effects. The correct ordering is important. Default is a vector full of

random effects. The correct ordering is important. Default is a vector full of

zeros.

index vector which defines the grouping of the variables. Components sharing the

same number build a group and factor variables get a single number (and are automatically treated as a group). Non-penalized coefficients are marked with

q_start a scalar or matrix of suitable dimension, specifying starting values for the random-

> effects variance-covariance matrix. Default is a scalar 0.1 or diagonal matrix with 0.1 in the diagonal, depending on the dimension of the random effects.

controls the speed of convergence. Default is 1e-3. conv.eps

a list specifying the number of basis functions nbasis (used for the baseline smooth

> hazard and all time-varying effects) and the starting value for the smoothness penalty parameter penal, which is only applied in the first iteration. Then, in all following iterations the wiggly components of the smooths are treated as random

effects. The degree of the B-splines is fixed to be three (i.e. cubic splines).

standardize logical. If true, the covariates corresponding to the fixed effects will be scaled

to a variance equal to one. Default is TRUE.

logical. If true, the covariates corresponding to the time-varying effects will center

> be centered. Default is FALSE (and centering is only recommended if really necessary; it can also have a strong effect on the baseline hazard, in particular,

if a strong penalty is selected).

print.iter logical. Should the number of iterations be printed? Default is FALSE.

max.iter the number of iterations for the final Fisher scoring re-estimation procedure.

Default is 200.

exact	controls the exactness of the (Riemann) integral approximations. If not set by the user to a specific value, it will be automatically chosen such that the time interval [0,t_max] will be divided in about 1000 equal sized Riemann bars.
xr	maximal time point that is regarded. Default is NULL and the maximal event or censoring time point in the data is used.
eps	Small epsilon that controls which fixed effects are set to zero: parameters with an absolute value smaller than epsilon are taken to be zero. Default is 1e-3.
	Futher arguments to be passed.

Value

a list with components for each of the possible arguments.

Author(s)

```
Andreas Groll groll@math.lmu.de>
```

See Also

coxFL

Examples

```
# Use different weighting of the two penalty parts
# and lighten the convergence criterion
coxFLControl(c.app = 1e-5, conv.eps=1e-3)
```

coxlasso

A LASSO approach for Cox Frailty Models.

Description

A LASSO approach for Cox Frailty Models based on the Cox full likelihood is provided.

Usage

Arguments

fix

a two-sided linear formula object describing the LASSO-penalized fixed (time-constant) effects part of the model, with the response on the left of a ~ operator and the terms, separated by + operators, on the right. The response must be a survival object as returned by the Surv function.

rnd a two-sided linear formula object describing the random-effects part of the model, with the grouping factor on the left of a ~ operator and the random terms, sep-

arated by + operators, on the right. Default is NULL, so no random effects are

present.

vary.coef a one-sided linear formula object describing the time-varying effects part of the

model, with the time-varying terms, separated by + operators, on the right side of a ~ operator. Default is NULL, so no time-varying effects are incorporated.

data the data frame containing the variables named in the three preceding formula

arguments.

xi the LASSO-penalty parameter that controls the strenght of the penalty term. The

optimal penalty parameter is a tuning parameter of the procedure that has to be determined, e.g. by K-fold cross validation (see cv.coxlasso for details or the

quick demo for an example).

adaptive.weights

for the LASSO-penalized fixed effects a vector of adaptive weights can be passed to the procedure. If no adaptive weights are specified, an unpenalized model (i.e. $\xi=0$) is fitted by the coxFL function and the obtained estimates are used

as adaptive weights (see value section).

control a list of control values for the estimation algorithm to replace the default values

returned by the function coxlassoControl. Defaults to an empty list.

Details

The coxlasso algorithm is designed to investigate the effect structure in the Cox frailty model, which is a widely used model that accounts for heterogeneity in time-to-event data. Since in survival models one has to account for possible variation of the effect strength over time, some features can incorporated with time-varying effects.

The penalty is depending on the LASSO tuning parameter ξ , which has to be determined by a suitable technique, e.g. by K-fold cross validation.

Package: pencoxfrail
Type: Package
Version: 1.1.2
Date: 2023-08-25
License: GPL-2
LazyLoad: yes

for loading a dataset type data(nameofdataset)

Value

Generic functions such as print, predict, plot and summary have methods to show the results of the fit.

The predict function uses also estimates of random effects for prediction, if possible (i.e. for known subjects of the grouping factor). Either the survival stepfunction or the baseline hazard (not cumulative!) can be calculated by specifying one of two possible methods: method=c("hazard", "survival").

By default, for each new subject in new.data an individual stepfunction is calculated on a prespecified time grid, also accounting for covariate changes over time. Alternatively, for new.data a single vector of a specific (time-constant) covariate combination can be specified.

Usage: predict(coxlasso.obj,new.data,time.grid,method=c("hazard","survival"))

The plot function plots all time-varying effects, including the baseline hazard.

a list containing an image of the coxlasso call that produced the object. call

baseline a vector containing the estimated B-spline coefficients of the baseline hazard. If

> the covariates corresponding to the time-varying effects are centered (and standardized, see coxlassoControl), the coefficients are transformed back to the

original scale.

a vector containing the estimated B-spline coefficients of all time-varying eftime.vary

> fects. If the covariates corresponding to the time-varying effects are standardized (see coxlassoControl) the coefficients are transformed back to the origi-

nal scale.

coefficients a vector containing the estimated fixed effects.

a vector containing the estimated random effects. ranef

0 a scalar or matrix containing the estimates of the random effects standard devi-

ation or variance-covariance parameters, respectively.

Delta a matrix containing the estimates of fixed and random effects (columns) for each

iteration (rows) of the main algorithm (i.e. before the final re-estimation step is

performed, see details).

Q_long a list containing the estimates of the random effects variance-covariance param-

eters for each iteration of the main algorithm.

iter number of iterations until the main algorithm has converged.

adaptive.weights

if not given as an argument by the user, a two-column matrix of adaptive weights

is calculated by the coxFL function; the first column contains the weights $w_{\Delta,k}$,

the second column the weights v_k from $\xi \cdot J(\zeta, \alpha)$.

knots vector of knots used in the B-spline representation.

large B-spline design matrix corresponding to the baseline hazard and all time-Phi.big

> varying effects. For the time-varying effects, the B-spline functions (as a function of time) have already been multiplied with their associated covariates.

time.grid the time grid used in when approximating the (Riemann) integral involved in the

model's full likelihood.

m number of metric covariates with time-varying effects.

m₂number of categorical covariates with time-varying effects.

Author(s)

Andreas Groll <groll@statistik.tu-dortmund.de> Maike Hohberg <mhohber@uni-goettingen.de>

References

Groll, A., T. Hastie and G. Tutz (2017). Selection of Effects in Cox Frailty Models by Regularization Methods. *Biometrics* 73(3): 846-856.

See Also

```
coxlassoControl,cv.coxlasso,coxFL,Surv,pbc
```

```
## Not run:
data(lung)
# remove NAs
lung <- lung[!is.na(lung$inst),]</pre>
# transform inst into factor variable
lung$inst <- as.factor(lung$inst)</pre>
# just for illustration, create factor with only three ph.ecog classes
lung$ph.ecog[is.na(lung$ph.ecog)] <- 2</pre>
lung$ph.ecog[lung$ph.ecog==3] <- 2</pre>
lung$ph.ecog <- as.factor(lung$ph.ecog)</pre>
fix.form <- as.formula("Surv(time, status) ~ 1 + age + ph.ecog + sex")</pre>
lasso.obj <- coxlasso(fix=fix.form, data=lung, xi=10,</pre>
                 control=list(print.iter=TRUE, exact = 1))
coef(lasso.obj)
# now add random institutional effect
lasso.obj2 <- coxlasso(fix=fix.form, rnd = list(inst=~1),</pre>
               data=lung, xi=10,control=list(print.iter=TRUE, exact = 1))
coef(lasso.obj2)
# print frailty Std.Dev.
print(lasso.obj2$Q)
# print frailties
print(lasso.obj2$ranef)
# now fit a time-varying effect for age
fix.form <- as.formula("Surv(time, status) ~ 1 + ph.ecog + sex")</pre>
vary.coef <- as.formula("~ age")</pre>
lasso.obj3 <- coxlasso(fix=fix.form,vary.coef=vary.coef,</pre>
               data=lung, xi=10,control=list(print.iter=TRUE))
summary(lasso.obj3)
# show fit
plot(lasso.obj3)
```

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```
# predict survival curve of new subject, institution 1 and up to time 300
pred.obj <- predict(lasso.obj2, newdata=data.frame(inst=1, time=NA, status=NA, age=26,</pre>
              ph.ecog=2, sex=1), time.grid=seq(0,300,by=1))
# plot predicted hazard function
plot(pred.obj$time.grid,pred.obj$haz,type="l",xlab="time",ylab="hazard")
# plot predicted survival function
plot(pred.obj$time.grid,pred.obj$survival,type="1",xlab="time",ylab="survival")
## specify a larger new data set
new.data \leftarrow data.frame(inst=c(1,1,6), time=c(20,40,200),
      status=c(NA,NA,NA), age=c(26,26,54), ph.ecog=c(0,0,2), sex=c(1,1,1))
## as here no frailties have been specified, id.var needs to be given!
pred.obj2 <- predict(lasso.obj3, newdata=new.data,id.var = "inst")</pre>
# plot predicted hazard functions (for the available time intervals)
plot(pred.obj2$time.grid[!is.na(pred.obj2$haz[,1])],
      pred.obj2$haz[,1][!is.na(pred.obj2$haz[,1])],
      type="1",xlab="time",ylab="hazard",xlim=c(0,200),
      ylim=c(0,max(pred.obj2$haz,na.rm=T)))
lines(pred.obj2$time.grid[!is.na(pred.obj2$haz[,3])],
      pred.obj2$haz[,3][!is.na(pred.obj2$haz[,3])],
      col="red",lty=2,)
# plot predicted survival functions (for the available time intervals)
plot(pred.obj2$time.grid[!is.na(pred.obj2$survival[,1])],
    pred.obj2$survival[,1][!is.na(pred.obj2$survival[,1])],
    type="1",xlab="time",ylab="hazard",xlim=c(0,200),
    ylim=c(0,max(pred.obj2$survival,na.rm=T)))
lines(pred.obj2$time.grid[!is.na(pred.obj2$survival[,3])],
      pred.obj2$survival[,3][!is.na(pred.obj2$survival[,3])],
      col="red", lty=2,)
# see also demo("coxlasso-lung")
## End(Not run)
```

coxlassoControl

Control Values for coxlasso fit

Description

The values supplied in the function call replace the defaults and a list with all possible arguments is returned. The returned list is used as the control argument to the coxlasso function.

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Usage

Arguments

start a vector of suitable length containing starting values for the spline-coefficients

of the baseline hazard and the time-varying effects, followed by the fixed and random effects. The correct ordering is important. Default is a vector full of

zeros.

index vector which defines the grouping of the variables. Components sharing the

same number build a group and factor variables get a single number (and are automatically treated as a group). Non-penalized coefficients are marked with

NA.

q_start a scalar or matrix of suitable dimension, specifying starting values for the random-

effects variance-covariance matrix. Default is a scalar 0.1 or diagonal matrix with 0.1 in the diagonal, depending on the dimension of the random effects.

conv.eps controls the speed of convergence. Default is 1e-3.

center logical. If true, the covariates corresponding to the time-varying effects will

be centered. Default is FALSE (and centering is only recommended if really necessary; it can also have a strong effect on the baseline hazard, in particular,

if a strong penalty is selected).

standardize logical. If true, the covariates corresponding to the fixed effects will be scaled

to a variance equal to one. Default is TRUE.

smooth a list specifying the number of basis functions nbasis (used for the baseline haz-

ard and all time-varying effects) and the smoothness penalty parameter penal, which is only applied to the baseline hazard. All time-varying effects are penalized by the specific double-penalty $\xi \cdot J(\zeta, \alpha)$ (see coxlasso), which is based on the overall penalty parameter ξ (specified in the main function coxlasso) and on the weighting between the two penalty parts ζ . The degree of the B-splines

is fixed to be three (i.e. cubic splines).

print.iter logical. Should the number of iterations be printed? Default is FALSE.

max.iter the number of iterations for the final Fisher scoring re-estimation procedure.

Default is 200.

c.app The parameter controlling the exactness of the quadratic approximations of the

penalties. Default is 1e-6.

exact controls the exactness of the (Riemann) integral approximations. If not set by

the user to a specific value, it will be automatically chosen such that the time interval [0,t_max] will be divided in about 1000 equal sized Riemann bars.

xr maximal time point that is regarded. Default is NULL and the maximal event or

censoring time point in the data is used.

eps Small epsilon that controls which fixed effects are set to zero: parameters with

an absolute value smaller than epsilon are taken to be zero. Default is 1e-2.

quant.knots Shall the knots be defined based on quantiles? Default is TRUE.

.

... Futher arguments to be passed.

Value

a list with components for each of the possible arguments.

Author(s)

Andreas Groll <groll@math.lmu.de>

See Also

coxlasso

Examples

```
# Use different weighting of the two penalty parts
# and lighten the convergence criterion
coxlassoControl(c.app = 1e-5, conv.eps=1e-3)
```

coxridge

A ridge approach for Cox Frailty Models.

Description

A ridge regression approach for Cox Frailty Models based on the Cox full likelihood is provided.

Usage

```
coxridge(fix=formula, rnd=NULL, vary.coef=NULL, xi.ridge, data, control = list())
```

Arguments

fix a two-sided linear formula object describing the LASSO-penalized fixed (time-

constant) effects part of the model, with the response on the left of a ~ operator and the terms, separated by + operators, on the right. The response must be a

survival object as returned by the Surv function.

rnd a two-sided linear formula object describing the random-effects part of the model,

with the grouping factor on the left of a \sim operator and the random terms, separated by + operators, on the right.Default is NULL, so no random effects are

present.

a one-sided linear formula object describing the time-varying effects part of the model, with the time-varying terms, separated by + operators, on the right side of a ~ operator.Default is NULL, so no time-varying effects are incorporated.

xi.ridge the ridge-penalty parameter that controls the strenght of the penalty term. The optimal penalty parameter is a tuning parameter of the procedure that has to be determined, e.g. by K-fold cross validation.

data the data frame containing the variables named in the three preceding formula arguments.

control a list of control values for the estimation algorithm to replace the default values returned by the function coxlassoControl. Defaults to an empty list.

Details

The coxridge algorithm is designed to investigate the effect structure in the Cox frailty model, which is a widely used model that accounts for heterogeneity in time-to-event data. Since in survival models one has to account for possible variation of the effect strength over time, some features can incorporated with time-varying effects.

The penalty is depending on the ridge tuning parameter ξ ridge, which has to be determined by a suitable technique, e.g. by K-fold cross validation.

Package: pencoxfrail
Type: Package
Version: 1.1.2
Date: 2023-08-25
License: GPL-2
LazyLoad: yes

for loading a dataset type data(nameofdataset)

Value

Generic functions such as print, predict, plot and summary have methods to show the results of the fit.

The predict function uses also estimates of random effects for prediction, if possible (i.e. for known subjects of the grouping factor). Either the survival stepfunction or the baseline hazard (not cumulative!) can be calculated by specifying one of two possible methods: method=c("hazard", "survival"). By default, for each new subject in new.data an individual stepfunction is calculated on a prespecified time grid, also accounting for covariate changes over time. Alternatively, for new.data a single vector of a specific (time-constant) covariate combination can be specified.

Usage: predict(coxlasso.obj,new.data,time.grid,method=c("hazard","survival"))

The plot function plots all time-varying effects, including the baseline hazard.

call a list containing an image of the coxlasso call that produced the object.

baseline a vector containing the estimated B-spline coefficients of the baseline hazard. If

the covariates corresponding to the time-varying effects are centered (and standardized, see coxlassoControl), the coefficients are transformed back to the

original scale.

time.vary a vector containing the estimated B-spline coefficients of all time-varying ef-

fects. If the covariates corresponding to the time-varying effects are standardized (see coxlassoControl) the coefficients are transformed back to the original control of the coefficients are transformed back to the original control of the coefficients are transformed back to the original control of the coefficients are transformed back to the original coefficient are transformed back to the original

nal scale.

coefficients a vector containing the estimated fixed effects.

ranef a vector containing the estimated random effects.

Q a scalar or matrix containing the estimates of the random effects standard devi-

ation or variance-covariance parameters, respectively.

Delta a matrix containing the estimates of fixed and random effects (columns) for each

iteration (rows) of the main algorithm (i.e. before the final re-estimation step is

performed, see details).

Q_long a list containing the estimates of the random effects variance-covariance param-

eters for each iteration of the main algorithm.

iter number of iterations until the main algorithm has converged.

adaptive.weights

if not given as an argument by the user, a two-column matrix of adaptive weights is calculated by the coxFL function; the first column contains the weights $w_{\Delta,k}$,

the second column the weights v_k from $\xi \cdot J(\zeta, \alpha)$.

knots vector of knots used in the B-spline representation.

Phi.big large B-spline design matrix corresponding to the baseline hazard and all time-

varying effects. For the time-varying effects, the B-spline functions (as a function of time) have already been multiplied with their associated covariates.

time.grid the time grid used in when approximating the (Riemann) integral involved in the

model's full likelihood.

m number of metric covariates with time-varying effects.
 m2 number of categorical covariates with time-varying effects.

Author(s)

Andreas Groll Groll Groll@statistik.tu-dortmund.de> Maike Hohberg <mhohber@uni-goettingen.de>

References

Groll, A., T. Hastie and G. Tutz (2017). Selection of Effects in Cox Frailty Models by Regularization Methods. *Biometrics* 73(3): 846-856.

See Also

```
coxlassoControl,cv.coxlasso,coxFL,Surv,pbc
```

```
## Not run:
# remove NAs
lung <- lung[!is.na(lung$inst),]</pre>
```

```
# transform inst into factor variable
lung$inst <- as.factor(lung$inst)</pre>
# just for illustration, create factor with only three ph.ecog classes
lung$ph.ecog[is.na(lung$ph.ecog)] <- 2</pre>
lung$ph.ecog[lung$ph.ecog==3] <- 2</pre>
lung$ph.ecog <- as.factor(lung$ph.ecog)</pre>
fix.form <- as.formula("Surv(time, status) ~ 1 + age + ph.ecog + sex")</pre>
ridge.obj <- coxridge(fix=fix.form, data=lung, xi.ridge=10,</pre>
                control=list(print.iter=TRUE, exact = 1))
coef(ridge.obj)
# now add random institutional effect
ridge.obj2 <- coxridge(fix=fix.form, rnd = list(inst=~1),</pre>
              data=lung, xi.ridge=10,control=list(print.iter=TRUE, exact = 1))
coef(ridge.obj2)
# print frailty Std.Dev.
print(ridge.obj2$Q)
# print frailties
print(ridge.obj2$ranef)
# now fit a time-varying effect for age
fix.form <- as.formula("Surv(time, status) ~ 1 + ph.ecog + sex")</pre>
vary.coef <- as.formula("~ age")</pre>
ridge.obj3 <- ridgelasso(fix=fix.form,vary.coef=vary.coef,</pre>
              data=lung, xi.ridge=10,control=list(print.iter=TRUE))
summary(ridge.obj3)
# show fit
plot(ridge.obj3)
# predict survival curve of new subject, institution 1 and up to time 300
pred.obj <- predict(ridge.obj2, newdata=data.frame(inst=1, time=NA, status=NA, age=26,</pre>
              ph.ecog=2, sex=1), time.grid=seq(0,300,by=1))
# plot predicted hazard function
plot(pred.obj$time.grid,pred.obj$haz,type="l",xlab="time",ylab="hazard")
# plot predicted survival function
plot(pred.obj$time.grid,pred.obj$survival,type="1",xlab="time",ylab="survival")
## specify a larger new data set
new.data <- data.frame(inst=c(1,1,6), time=c(20,40,200),
      status=c(NA,NA,NA), age=c(26,26,54), ph.ecog=c(0,0,2), sex=c(1,1,1))
## as here no frailties have been specified, id.var needs to be given!
pred.obj2 <- predict(lasso.obj3, newdata=new.data,id.var = "inst")</pre>
```

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```
# plot predicted hazard functions (for the available time intervals)
plot(pred.obj2$time.grid[!is.na(pred.obj2$haz[,1])],
      pred.obj2$haz[,1][!is.na(pred.obj2$haz[,1])],
      type="1",xlab="time",ylab="hazard",xlim=c(0,200),
      ylim=c(0,max(pred.obj2$haz,na.rm=T)))
lines(pred.obj2$time.grid[!is.na(pred.obj2$haz[,3])],
      pred.obj2$haz[,3][!is.na(pred.obj2$haz[,3])],
      col="red",lty=2,)
# plot predicted survival functions (for the available time intervals)
plot(pred.obj2$time.grid[!is.na(pred.obj2$survival[,1])],
    pred.obj2$survival[,1][!is.na(pred.obj2$survival[,1])],
    type="1",xlab="time",ylab="hazard",xlim=c(0,200),
    ylim=c(0,max(pred.obj2$survival,na.rm=T)))
lines(pred.obj2$time.grid[!is.na(pred.obj2$survival[,3])],
      pred.obj2$survival[,3][!is.na(pred.obj2$survival[,3])],
      col="red",lty=2,)
# see also demo("coxlasso-lung")
## End(Not run)
```

cv.coxlasso

Cross-validation for coxlasso

Description

performs k-fold cross-validation for coxlasso, produces a plot, and returns a value for the LASSO tuning parameter ξ .

Usage

Arguments

fix

a two-sided linear formula object describing the fixed (time-constant) effects part of the model, with the response on the left of a \sim operator and the terms, separated by + operators, on the right. The response must be a survival object as returned by the Surv function.

rnd

a two-sided linear formula object describing the random-effects part of the model, with the grouping factor on the left of a \sim operator and the random terms, separated by + operators, on the right. Default is NULL, so no random effects are present.

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vary.coef	a one-sided linear formula object describing the time-varying effects part of the model, with the time-varying terms, separated by + operators, on the right side of a ~ operator. Default is NULL, so no time-varying effects are incorporated.
n.folds	number of folds. Default is 10.
хi	Optional user-supplied xi sequence; default is NULL, and cv.coxlasso chooses its own sequence
data	the data frame containing the variables named in the three preceding formula arguments.
adaptive.weigh	ts
	for the LASSO-penalized fixed effects a vector of adaptive weights can be passed to the procedure. If no adaptive weights are specified, an unpenalized model (i.e. $\xi=0$) is fitted by the coxFL function and the obtained estimates are used as adaptive weights (see value section).
print.fold	Should folds of CV be printed? Default is yes.
print.xi	Should current ξ value be printed? Default is no.
len.xi	Length of ξ grid. Default is 100.
lgrid	Logical; shall a logarithmized grid version for the penalty parameter be used? Default is TRUE.
ran.seed	Random seed number to be set. Default is 1909, the year of birth of Borussia Dortmund football club.
xi.factor	A factor which increases xi.max once again to be sure that xi is large enough on all sets. Default is 1.01
min.fold	Only those xi values are taken into account where at least min.fold folds are not NA. Default is 4.
pass.on.start	Shall starting values be passed onthroughout estimation? Default is TRUE
control	a list of control values for the estimation algorithm to replace the default values returned by the function coxlassoControl. Default is print.iter = FALSE.

Details

The function runs coxlasso over a grid of values ξ for each training data set with one fold omitted. For each run, the value for the full likelihood is calculated and the average for each ξ on the grid is computed over the folds. The function choses the ξ that maximizes this likelihood value as the optimal tuning parameter value.

Value

The function returns a list "cv.coxlasso" which includes:

cv.error	a vector of mean CV error (i.e., negative likelihood) values for each ξ on the grid averaged over the folds.
xi.opt	a scalar value of ξ associated with the smallest CV error.
xi.1se	largest value of ξ such that error is within 1 standard error of the minimum.

The plot function plots the values of ξ against the corresponding CV error (i.e., negative likelihood) values.

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Author(s)

References

To appear soon.

See Also

```
coxlasso, coxlassoControl, coxFL, Surv, pbc
```

```
## Not run:
data(lung)
# remove NAs
lung <- lung[!is.na(lung$inst),]</pre>
# transform inst into factor variable
lung$inst <- as.factor(lung$inst)</pre>
# just for illustration, create factor with only three ph.ecog classes
lung$ph.ecog[is.na(lung$ph.ecog)] <- 2</pre>
lung$ph.ecog[lung$ph.ecog==3] <- 2</pre>
lung$ph.ecog <- as.factor(lung$ph.ecog)</pre>
fix.form <- as.formula("Surv(time, status) ~ 1 + age + ph.ecog + sex")</pre>
# find optimal tuning paramater
cv.coxlasso.obj <- cv.coxlasso(fix = fix.form, data = lung, n.folds = 5)</pre>
# estimate coxlasso model with optimal xi
lasso.obj <- coxlasso(fix=fix.form, data=lung, xi=cv.coxlasso.obj$xi.opt,</pre>
                 control=list(print.iter=TRUE))
coef(lasso.obj)
# see also demo("coxlasso-lung")
## End(Not run)
```

int.approx 21

Description

The function approximates the integral $\int_0^t exp(uB(s)\alpha)ds$) which appears in the (full) Cox likelihood if the covariate u has a time-varying effect $\beta(t)$, which is expanded in B-splines, i.e. $\beta(t)=B(t)\alpha$.

Usage

```
int.approx(z,time.grid,B,nbasis,alpha)
```

Arguments

z	a vector which contains at the first component a time point up to which it should be integrated and the covariates \boldsymbol{u} in the remaining components.
time.grid	an equally-spaced time grid on which the B-spline design matrix B has been generated. The maximal value of the time grid should usually be the maximal upper integral border that is of interest.
В	a B-spline design matrix, which has been created with the function bs.design on the full time grid time.grid.
nbasis	number of basis functions used when the B-spline design matrix \boldsymbol{B} has been generated.
alpha	vector of B-spline coefficients.

Value

The B-spline design matrix is returned.

Author(s)

```
Andreas Groll <groll@math.lmu.de>
```

See Also

```
pencoxfrail
```

```
## generate time grid and corresponding B-spline design matrix
time.grid <- seq(0,200,by=1)
B <- bs.design(x=time.grid, xl=min(time.grid), xr=max(time.grid), spline.degree=3, nbasis=5)

## specify spline coefficients and covariate vector (with upper integral bound as first component)
alpha <- c(0.1,0.2,0.05,0.1,0.15)
z <- c(time=100,age=25)

## calculate intergal from 0 to 100
int.approx(z=z,time.grid=time.grid,B=B,nbasis=5,alpha=alpha)</pre>
```

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|--|

Description

A regularization approach for Cox Frailty Models by penalization methods is provided.

Usage

Arguments

vary.coef

data

хi

fix	a two-sided linear formula object describing the unpenalized fixed (time-constant) effects part of the model, with the response on the left of a ~ operator and the terms, separated by + operators, on the right. The response must be a survival object as returned by the Surv function.	
rnd	a two-sided linear formula object describing the random-effects part of the model,	

with the grouping factor on the left of a ~ operator and the random terms, separated by + operators, on the right.

a one-sided linear formula object describing the time-varying effects part of the model, with the time-varying terms, separated by + operators, on the right side of a ~ operator.

the data frame containing the variables named in the three preceding formula arguments.

the overall penalty parameter that controls the strenght of both penalty terms in $\xi \cdot J(\zeta, \alpha)$ and, hence, controls the overall amount of smoothness (up to constant effects) and variable selection for a given proportion ζ . The optimal penalty parameter is a tuning parameter of the procedure that has to be determined, e.g. by K-fold cross validation. (See details or the quick demo for an example.)

adaptive.weights

a two-column matrix of adaptive weights passed to the procedure; the first column contains the weights $w_{\Delta,k}$, the second column the weights v_k from $\xi \cdot J(\zeta,\alpha)$. If no adaptive weights are specified all weights are set to one. The recommended strategy is to first fit an unpenalized model (i.e. $\xi=0$) and then use the obtained adaptive weights (see value section) when fitting the model for all other combinations of ξ and ζ .

a list of control values for the estimation algorithm to replace the default values returned by the function pencoxfrailControl. Defaults to an empty list.

Details

control

The pencoxfrail algorithm is designed to investigate the effect structure in the Cox frailty model, which is a widely used model that accounts for heterogeneity in survival data. Since in survival

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models one has to account for possible variation of the effect strength over time the selection of the relevant features distinguishes between the following cases: covariates can have time-varying effects, can have time-constant effects or be irrelevant. For this purpose, the following specific penality is applied on the vectors of B-spline coefficients α_k , assuming k=1,...,r different, potentially time-varying effects, each expanded in M B-spline basis functions:

$$\xi \cdot J(\zeta, \alpha) = \xi \left(\zeta \sum_{k=1}^{r} \psi w_{\Delta,k} ||\Delta_M \alpha_k||_2 + (1 - \zeta) \sum_{k=1}^{r} \phi v_k ||\alpha_k||_2 \right)$$

This penalty is able to distinguish between these types of effects to obtain a sparse representation that includes the relevant effects in a proper form.

The penalty is depending on two tuning parameters, ξ and ζ , which have to be determined by a suitable technique, e.g. by (2-dimensional) K-fold cross validation.

The first term of the penalty controls the smoothness of the time-varying covariate effects, whereby for values of ξ and ζ large enough, all differences $(\alpha_{k,l}-\alpha_{k,l-1}), l=2,...,M$, are removed from the model, resulting in constant covariate effects. As the B-splines of each variable with varying coefficients sum up to one, a constant effect is obtained if all spline coefficients are set equal. Hence, the first penalty term does not affect the spline's global level. The second term penalizes all spline coefficients belonging to a single time-varying effect in the way of a group LASSO and, hence, controls the selection of covariates.

Package: pencoxfrail
Type: Package
Version: 1.1.2
Date: 2023-08-25
License: GPL-2
LazyLoad: yes

for loading a dataset type data(nameofdataset)

Value

Generic functions such as print, predict, plot and summary have methods to show the results of the fit.

The predict function uses also estimates of random effects for prediction, if possible (i.e. for known subjects of the grouping factor). Either the survival stepfunction or the baseline hazard (not cumulative!) can be calculated by specifying one of two possible methods: method=c("hazard", "survival"). By default, for each new subject in new.data an individual stepfunction is calculated on a prespecified time grid, also accounting for covariate changes over time. Alternatively, for new.data a single vector of a specific (time-constant) covariate combination can be specified.

Usage: predict(pencoxfrail.obj,new.data,time.grid,method=c("hazard","survival"))

The plot function plots all time-varying effects, including the baseline hazard.

call a list containing an image of the pencoxfrail call that produced the object.

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baseline a vector containing the estimated B-spline coefficients of the baseline hazard. If

the covariates corresponding to the time-varying effects are centered (and standardized, see pencoxfrailControl), the coefficients are transformed back to

the original scale.

time.vary a vector containing the estimated B-spline coefficients of all time-varying ef-

fects. If the covariates corresponding to the time-varying effects are standardized (see pencoxfrailControl) the coefficients are transformed back to the

original scale.

coefficients a vector containing the estimated fixed effects.

ranef a vector containing the estimated random effects.

Q a scalar or matrix containing the estimates of the random effects standard devi-

ation or variance-covariance parameters, respectively.

Delta a matrix containing the estimates of fixed and random effects (columns) for each

iteration (rows) of the main algorithm (i.e. before the final re-estimation step is

performed, see details).

Q_long a list containing the estimates of the random effects variance-covariance param-

eters for each iteration of the main algorithm.

iter number of iterations until the main algorithm has converged.

adaptive.weights

If $\xi=0$, a two-column matrix of adaptive weights is calculated; the first column contains the weights $w_{\Delta,k}$, the second column the weights v_k from $\xi \cdot J(\zeta,\alpha)$. If $\xi>0$, the adaptive weights that have been used in the function's argument

are displayed.

knots vector of knots used in the B-spline representation.

Phi.big large B-spline design matrix corresponding to the baseline hazard and all time-

varying effects. For the time-varying effects, the B-spline functions (as a function of time) have already been multiplied with their associated covariates.

time.grid the time grid used in when approximating the (Riemann) integral involved in the

model's full likelihood.

m number of metric covariates with time-varying effects.

m2 number of categorical covariates with time-varying effects.

Author(s)

Andreas Groll <groll@math.lmu.de>

References

Groll, A., T. Hastie and G. Tutz (2017). Selection of Effects in Cox Frailty Models by Regularization Methods. *Biometrics* 73(3): 846-856.

See Also

pencoxfrailControl,Surv,pbc

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Examples

```
## Not run:
data(lung)
# remove NAs
lung <- lung[!is.na(lung$inst),]</pre>
# transform inst into factor variable
lung$inst <- as.factor(lung$inst)</pre>
# Random institutional effect
fix.form <- as.formula("Surv(time, status) ~ 1")</pre>
vary.coef <- as.formula("~ age")</pre>
pen.obj <- pencoxfrail(fix=fix.form,vary.coef=vary.coef, rnd = list(inst=~1),</pre>
              data=lung, xi=10,control=list(print.iter=TRUE))
# show fit
plot(pen.obj)
# predict survival curve of new subject, institution 1 and up to time 500
pred.obj <- predict(pen.obj,newdata=data.frame(inst=1,time=NA,status=NA,age=26),</pre>
               time.grid=seq(0,500,by=1))
# plot predicted hazard function
plot(pred.obj$time.grid,pred.obj$haz,type="l",xlab="time",ylab="hazard")
# plot predicted survival function
plot(pred.obj$time.grid,pred.obj$survival,type="1",xlab="time",ylab="survival")
# see also demo("pencoxfrail-pbc")
## End(Not run)
```

pencoxfrailControl

Control Values for pencoxfrail fit

Description

The values supplied in the function call replace the defaults and a list with all possible arguments is returned. The returned list is used as the control argument to the pencoxfrail function.

Usage

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Arguments

start a vector of suitable length containing starting values for the spline-coefficients of the baseline hazard and the time-varying effects, followed by the fixed and random effects. The correct ordering is important. Default is a vector full of zeros. q_start a scalar or matrix of suitable dimension, specifying starting values for the randomeffects variance-covariance matrix. Default is a scalar 0.1 or diagonal matrix with 0.1 in the diagonal, depending on the dimension of the random effects. conv.eps controls the speed of convergence. Default is 1e-4. center logical. If true, the covariates corresponding to the time-varying effects will be centered. Default is FALSE (and centering is only recommended if really necessary; it can also have a strong effect on the baseline hazard, in particular, if a strong penalty is selected). standardize logical. If true, the the covariates corresponding to the time-varying effects will be scaled to a variance equal to one (*after* possible centering). Default is FALSE. smooth a list specifying the number of basis functions nbasis (used for the baseline hazard and all time-varying effects) and the smoothness penalty parameter penal, which is only applied to the baseline hazard. All time-varying effects are penalized by the specific double-penalty $\xi \cdot J(\zeta, \alpha)$ (see pencoxfrail), which is based on the overall penalty parameter ξ (specified in the main function pencoxfrail) and on the weighting between the two penalty parts ζ. The degree of the Bsplines is fixed to be three (i.e. cubic splines). On all time-varying effects (except for the baseline hazard) a slight ridge penalty ridge.pen is applied on the second order differences of the corresponding spline coefficients to stabilize estimation. Default is 1e-4. print.iter logical. Should the number of iterations be printed? Default is FALSE. the number of iterations for the final Fisher scoring re-estimation procedure. max.iter Default is 200. The parameter controlling the exactness of the quadratic approximations of the c.app penalties. Default is 1e-6. The parameter controlling the weighting between the two penalty parts in the zeta specific double-penalty $\xi \cdot J(\zeta, \alpha)$ (see pencoxfrail). Default is 0.5. exact controls the exactness of the (Riemann) integral approximations. Default is 1emaximal time point that is regarded. Default is NULL and the maximal event or xr censoring time point in the data is used. Futher arguments to be passed.

Value

a list with components for each of the possible arguments.

Author(s)

Andreas Groll <groll@math.lmu.de>

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See Also

pencoxfrail

```
# Use different weighting of the two penalty parts
# and lighten the convergence criterion
pencoxfrailControl(zeta=0.3, conv.eps=1e-3)
```

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